

Wildcard Reconstruction

Tom Schrijvers

K.U.Leuven, Belgium
toms@cs.kuleuven.be

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IBM T.J. Watson Laboratory, Hawthorne, NY, USA





- 1 Research Background
- 2 Motivation
- 3 Framework
 - Algorithm
 - Properties
 - Extension: Cast Removal
- 4 Wildcard Inference
 - Algorithm Adaptations
- 5 Conclusion



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Constraint Logic Programming (CLP)

Ph.D. thesis 2005:

*Analyses, Optimizations and Extensions of
Constraint Handling Rules*

- ▶ program analysis (abstract interpretation)
- ▶ optimized compilation
- ▶ language extensions

CLP applied to type inference:

- ▶ Polymorphic ADT Reconstruction (PPDP 2006)
- ▶ Inference for Multi-Parameter Type Classes (APLAS 2006)

Constraint Handling Rules [Frühwirth'91]

- ▶ multi-set rewriting language
- ▶ for writing custom constraint solvers (and more)
- ▶ executable logic theory

Example

```
:- chr_constraint leq/2.  
  
    reflexive @ leq(X,X) <=> true.  
    antisymmetric @ leq(X,Y), leq(Y,X) <=> X = Y.  
    idempotent @ leq(X,Y) \ leq(X,Y) <=> true.  
    transitive @ leq(X,Y), leq(Y,Z) ==> leq(X,Z).
```

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```

?- $\frac{\text{leq}(A,B), \text{leq}(B,C)}{\text{leq}(A,B), \text{leq}(B,C), \text{leq}(C,A)}$, $\text{leq}(C,A)$ (trans.)
 \rightarrow $\frac{\text{leq}(A,B), \text{leq}(B,C), \text{leq}(C,A), \text{leq}(A,C)}{\text{leq}(A,B), \text{leq}(B,A), C = A}$ (anti)
 \rightarrow $\frac{\text{leq}(A,B), \text{leq}(B,A), C = A}{A = B, C = A}$ (anti)

Leuven Systems

- ▶ K.U.Leuven CHR (current main system)
 - ▶ Prolog: SWI-Prolog, SICStus, Yap, ...
 - ▶ JCHR in Java
 - ▶ CCHR in C
- ▶ language development
 - ▶ program analysis, termination
 - ▶ optimized compilation
 - ▶ language features: aggregates
- ▶ complexity results
 - ▶ RAM simulator
 - ▶ optimal in time & space

Applications

- ▶ study of constraint solvers (e.g. lexicographic) [Frühwirth]
- ▶ study of declarative algorithms:
 - ▶ compexity: union-find, dijkstra [Schrijvers]
 - ▶ parallel: union-find, preflow-push [Frühwirth]
- ▶ type systems:
 - ▶ inference, checking [Sulzmann,Schrijvers]
 - ▶ extensible type system [Sulzmann]
- ▶ more: agents, semantics web, NLP, verification, . . .
- ▶ programming language, e.g. SSS LTD, New Zealand



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Parametric Polymorphism for Java

- ▶ \leq Java 1.4:
 - ▶ monomorphic libraries,
e.g. `List list;`
 - ▶ many casts,
e.g. `Integer i = (Integer) list.first();`
 - ▶ statically **unchecked**
- ▶ Java 5: **generics**
 - ▶ polymorphic libraries,
e.g. `List<Integer> list;`
 - ▶ no/fewer casts
e.g. `Integer i = list.first();`
 - ▶ statically **checked**



Refactoring [Fowler'99]

Improving quality: adding generics to legacy Java code

- 1 **Library Code:** **little**
by hand (e.g. Java 5 libraries),
automatically [von Dincklage'04]
- 2 **Application Code:** **lots**
automatically [Donovan'04, Fuhrer'05]
 - ▶ optimal removal of casts?
 - ▶ wildcard types?



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Start simple...

Insights first

- ▶ variant of *Featherweight Java* [Igarashi et al.]
- ▶ simple type system: single inheritance, class types only, ...

...but flexible

Complexity and efficiency later

- ▶ extended language, extended type system
- ▶ grips on efficiency

The CLP Approach

- 1 determine unknowns (constraint variables)
- 2 determine constraints
- 3 rewrite constraints: propagate and simplify
- 4 any unknown left? pick one, *label* it and repeat 3

Unknown Type Parameters

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Introducing type parameters

- ▶ add parameter lists to all types in program
- ▶ a fresh unknown type α for every parameter

```
List meth(List l)
{
  return new List();
}
```

\Rightarrow

```
List< $\alpha$ > meth(List< $\beta$ > l)
{
  return new List< $\gamma$ >();
}
```

Type Constraints

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- ▶ subtyping ($<:$), e.g.

`Integer` $<:$ `Number`

- ▶ equality ($=$), e.g.

`Integer` $=$ `Integer`

Type Constraints: Implementation

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- ▶ `:- chr_constraint subtype/2.`
- ▶ `:- chr_constraint equal/2.`

Constraint Derivation

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$$(D-M) \frac{e_0.m(\bar{e}) \quad mtype(m, [e_0]) = \bar{U} \rightarrow U}{[\bar{e}] <: \bar{U}}$$

$$(D-RT) \frac{T \ m(\bar{T} \ \bar{x})\{ \mathbf{return} \ e; \}}{[e] <: T}$$

$$(D-Co) \frac{\mathbf{new} \ C\langle\bar{T}\rangle(\bar{e}) \quad fields(C\langle\bar{T}\rangle) = \bar{U} \ \bar{f};}{[\bar{e}] <: \bar{U}}$$

$$(D-BC) \frac{c\langle\bar{T}\rangle \quad \mathbf{class} \ C\langle\bar{X}\rangle \triangleleft \bar{B} \triangleleft N\{\dots\}}{\bar{T} <: \bar{B}}$$

Constraint Derivation: Implementation

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Example

$$(D-CO) \frac{\text{new } C\langle\bar{T}\rangle(\bar{e}) \quad \text{fields}(C\langle\bar{T}\rangle) = \bar{U} \bar{f};}{[\bar{e}] <: \bar{U}}$$

Prolog Implementation

```
derive(new(CT,Es),CT) :-
    maplist(derive,Es,TEs),
    field_types(CT,Us),
    maplist(subtype,TEs,Us).
```

Constraint Solving

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$$\text{solve} = \text{lfp}(\rightsquigarrow)$$

Rewriting the constraint store: $\sigma \rightsquigarrow \sigma'$

▶ simplify:

- ▶ trivial equations: $\{\alpha = \alpha\} \cup \sigma \rightsquigarrow \sigma$
- ▶ ground constraints: $\{c\} \cup \sigma \rightsquigarrow c$, if $uv(c) = \emptyset \wedge \vdash c$

▶ propagate:

- ▶ substitute equations: $\{\alpha = T\} \cup \sigma \rightsquigarrow \{\alpha = T\} \cup [T/\alpha]\sigma$
- ▶ add implied constraints: $\sigma \rightsquigarrow \sigma \cup \sigma'$, if $\sigma \vdash^P \sigma'$

▶ detect inconsistency: $\{c\} \cup \sigma \rightsquigarrow \text{fail}$, if $uv(c) = \emptyset \wedge \not\vdash c$

Constraint Solving: Implementation

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CHR Rules

```
equal(X,Y) <=> unify_with_occurs_check(X,Y).  
  
subtype(X,Y), subtype(Y,X) ==> equal(X,Y).  
  
subtype(X,Y), subtype(Y,Z) ==> subtype(X,Z).  
  
subtype(X,class(C,P1)), subtype(X,class(C,P2))  
    ==> equal(P1,P2).  
  
...
```

Labeling = eliminate unknown type

$$\sigma \mapsto \sigma \cup \{\alpha = T\}$$

- 1 **select variable:** pick a remaining unknown type α where $(\alpha = T) \notin \sigma$
- 2 **select value:** choose a candidate type to assign $\alpha = T_1$ where $\forall (L <: \alpha), (\alpha <: U) \in \sigma : L <: T_1 <: U$
- 3 **backtrack:** try different type upon failure $\alpha = T_2, T_3, \dots$

Desirable Properties

- ▶ **Soundness:** by construction type constraints are enforced
- ▶ **Completeness:** **problematic**
- ▶ **Termination:** depends on completeness

Infinite number of solutions!

Unconstrained unknown parameter α :

- ▶ $\alpha = \text{Object}$
- ▶ $\alpha = \text{List}\langle \text{Object} \rangle$
- ▶ $\alpha = \text{List}\langle \text{List}\langle \text{Object} \rangle \rangle$
- ▶ $\alpha = \text{List}\langle \text{List}\langle \text{List}\langle \text{Object} \rangle \rangle \rangle$
- ▶ ...

Completeness

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Solution: Label with upper bound

$$\alpha = \bigsqcap \{T \mid \alpha <: T\}$$

Advantages:

- ▶ it always exists (possibly Object)
- ▶ it is unique (least upper bound)
- ▶ it is sufficient to obtain a solution
- ▶ it makes the algorithm terminate

e.g. $\alpha = \bigsqcap \{\text{Integer}, \text{Number}, \text{Object}\} = \text{Integer}$

Cast Removal

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Goal: choose parameters to render casts redundant

In Java 1.4:

```
(Foo) new List().add(new Foo()).first()
```

becomes in Java 5:

```
(Foo) new List<Foo>().add(new Foo()).first()
```

or simply:

```
new List<Foo>().add(new Foo()).first()
```

Soft subtyping constraint

- ▶ derive soft constraint:

$$(D-CA) \frac{(N)_i e}{[e] \overset{\rightarrow}{<}_i N}$$

- ▶ consider soft constraints for labeling:

$$\alpha = (\bigsqcap \{T \mid \alpha <: T\}) \sqcap (\bigsqcap Sat)$$

where $Sat \subseteq \{T \mid \alpha \overset{\rightarrow}{<} T\}$

- ▶ best solution is optimal!



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Wildcard Types

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Problem: No variance for generic parameters

$$C\langle T \rangle <: C\langle S \rangle \Leftrightarrow T = S$$

Solution: wildcard types [Torgersen et al. 2004]

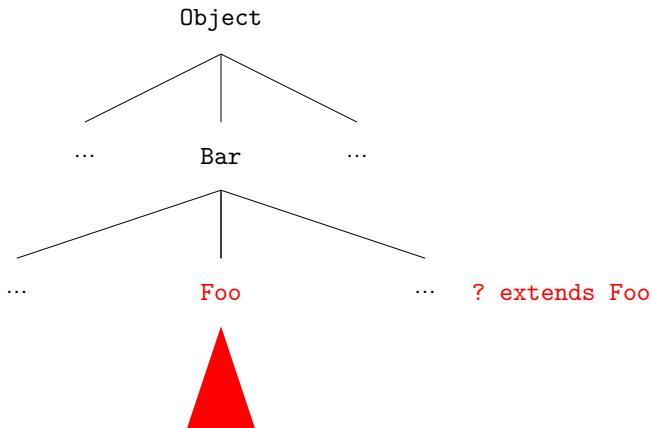
$$C\langle T \rangle <: C\langle S \rangle \Leftrightarrow T \subset: S$$

Three forms of wildcard parameters [JLS]:

- 1 unbounded: `?` (\equiv `? extends Object`)
- 2 bounded from above: `? extends Foo`
- 3 bounded from below: `? super Foo`

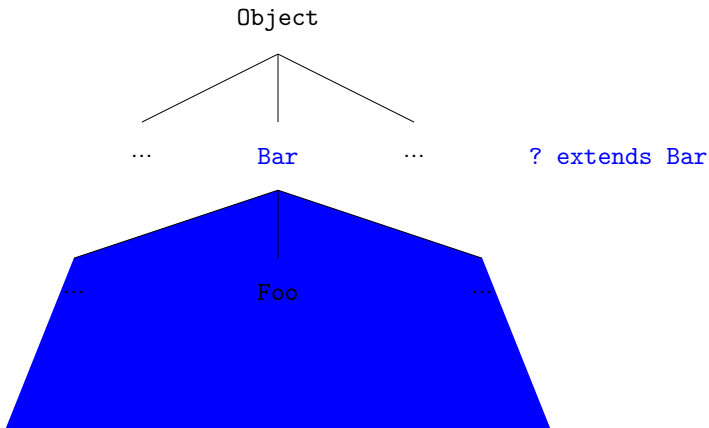
Wildcard Types = Type Ranges

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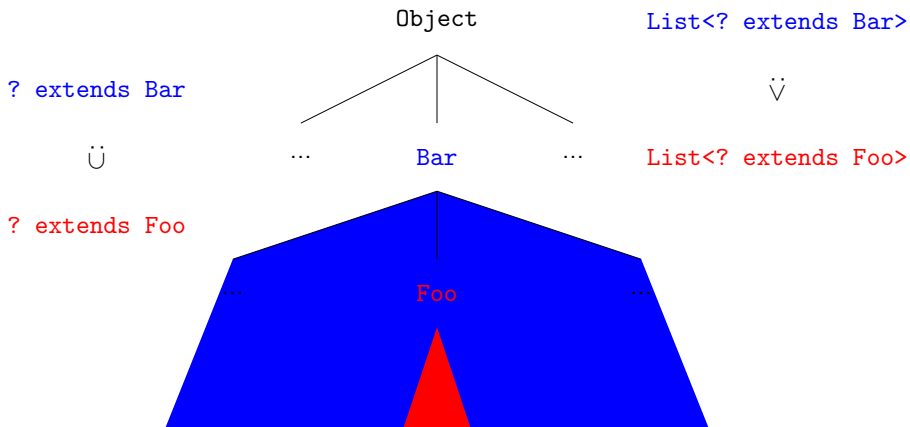
Wildcard Types = Type Ranges

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Range Containment \subset :

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Type Constraints

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- ▶ containment (\subset), e.g.

`? extends Integer` \subset `? extends Number`

- ▶ wildcard captures (*capture*), e.g.

capture(List<?>, List<X>)

- ▶ environment subtype (\prec), e.g.

`X` \prec Object where *capture*(List<?>, List<X>)

Constraint Derivation

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$$(D-M) \frac{T_{0,c} \text{ fresh} \quad \bar{T}_c \text{ fresh} \quad e_0.m(\bar{e}) \quad mtype(m, T_{0,c}) = \bar{U} \rightarrow U}{\text{capture}([e_0], T_{0,c}) \quad \text{capture}([\bar{e}], \bar{T}_c) \quad \bar{T}_c <: \bar{U}}$$

$$(D-RT) \frac{T \ m(\bar{T} \ \bar{x})\{ \text{return } e; \} \quad T_c \text{ fresh}}{\text{capture}([e], T_c) \quad T_c <: T}$$

$$(D-Co) \frac{\text{new } C\langle \bar{T} \rangle(\bar{e}) \quad \text{class } C\langle \bar{X} \triangleleft \bar{B} \rangle \triangleleft N\{\dots\} \quad \text{fields}(C\langle \bar{T} \rangle) = \bar{T}_f \ \bar{f} \quad \bar{T}_e \text{ fresh}}{\bar{T} <: \bar{B} \quad \text{nowildcard}(\bar{T}) \quad \text{capture}([\bar{e}], \bar{T}_e) \quad \bar{T}_e <: \bar{T}_f}$$

Additional propagation rules, e.g.

$$(\text{NoW-WLow}) \frac{\text{nowildcard}(? \triangleright T)}{\text{fail}}$$

$$(\text{NoW-WUP}) \frac{\text{nowildcard}(? \triangleleft T)}{\text{fail}}$$

Terminating

Only consider:

- 1 a class type as before
- 2 ? extends $\sqcap \{T \mid \alpha <: T\}$
- 3 ? super $\sqcup \{T \mid T <: \alpha\}$

No longer unique!

- ▶ multiple forms possible: 1-2 and 1-3
- ▶ non-unique lub/glb, e.g.

$$\sqcup \text{List}\langle \text{Number} \rangle, \text{List}\langle \text{Integer} \rangle = \\ \{ \text{List}\langle ? \text{ extends Number} \rangle, \text{List}\langle ? \text{ super Integer} \rangle \}$$



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Contributions

- 1 CLP-based framework for parameter inference
- 2 optimality of cast removal
- 3 inference of wildcards types

- ▶ extend the type language
 - ▶ **multiple inheritance**
 - ▶ covariant array types, primitive types, ...
- ▶ extend the problem scope
 - ▶ no distinction between libraries and applications
 - ▶ inference of non-parameter types
- ▶ optimize the solution (CLP algorithm)
 - ▶ add redundant propagation/simplification, faster failing
 - ▶ avoid redundant search: pruning
 - ▶ search heuristics: value/variable selection

Thank you

- ▶ questions?
- ▶ comments!